

# NEW SPECIMEN PAPERS PUBLISHED JUNE 2015

# GCSE Mathematics Specification (8300/2H)



Paper 2 Higher tier

Date

Morning

1 hour 30 minutes

### **Materials**

### For this paper you must have:

- a calculator
- · mathematical instruments.



### Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- · Fill in the boxes at the bottom of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book.
- In all calculations, show clearly how you work out your answer.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
   These must be tagged securely to this answer book.

Centre number				Cai	ndic	late	nu	mb	er						
Surname															
Forename(s)															
Candidate signa			٠												

## Answer all questions in the spaces provided.

Which sequence is a geometric progression?
Circle your answer.

[1 mark]

1 2 3 4

1 2 4 7



1 2 3 5

Which of these is **not** used to prove that triangles are congruent?
Circle your answer.

[1 mark]

SSS

SAS

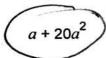


RHS

2002 + a

3 Circle the expression that is equivalent to  $2a + 5a \times 4a - a$ 

[1 mark]



 $21a^{2}$ 

$$28a^2 - a$$

$$2a + 15a^2$$

Circle the equation of a line that is parallel to y = 5x - 2

[1 mark]

$$y = 2x - 5$$

$$y = 5x + 2$$
  $y = 3x - 2$   $y = -\frac{1}{5}x - 2$ 

$$y = 3x - 2$$

$$y = -\frac{1}{5}x - 2$$

In a sale, the original price of a bag was reduced by  $\frac{1}{5} = 20$ , = 0.1The sale price of the bag is £29.40

Work out the original price.

[3 marks]

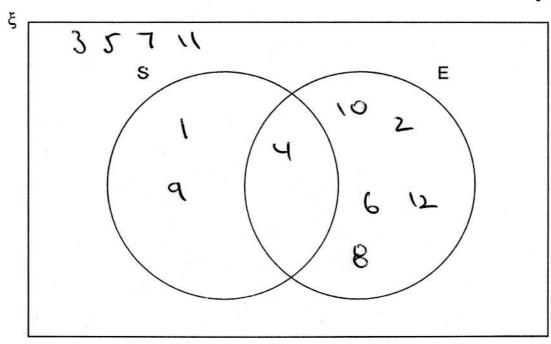
29.40 = 80'1. of Normal 29.40 = 01FN 36.95 = N -0.5

Answer £ 36.95 .

Turn over for the next question

- 6  $\xi = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$ 
  - S = square numbers
  - E = even numbers
- 6 (a) Complete the Venn diagram.

[3 marks]



- Prodobiliziry 6 (b) One of the numbers is chosen at random.

Write down  $P(S \cap E)$ 

[1 mark]

Answer

7 A coin is rolled onto a grid of squares.

It lands randomly on the grid.

To win, the coin must land completely within one of the squares.

Meera and John each roll the coin a number of times and record their results.

	Number of wins	Number of losses
Meera	6 .	44
John	28	72

7 (a) Work out two different estimates for the probability of winning.

[2 marks]

Meera 50 = 3

John. 28 = 14 2 7

Answer  $\frac{3}{15}$  and  $\frac{7}{15}$ 

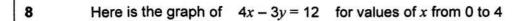
7 (b) Which of your estimates is the better estimate for the probability of winning?
Give a reason for your answer.

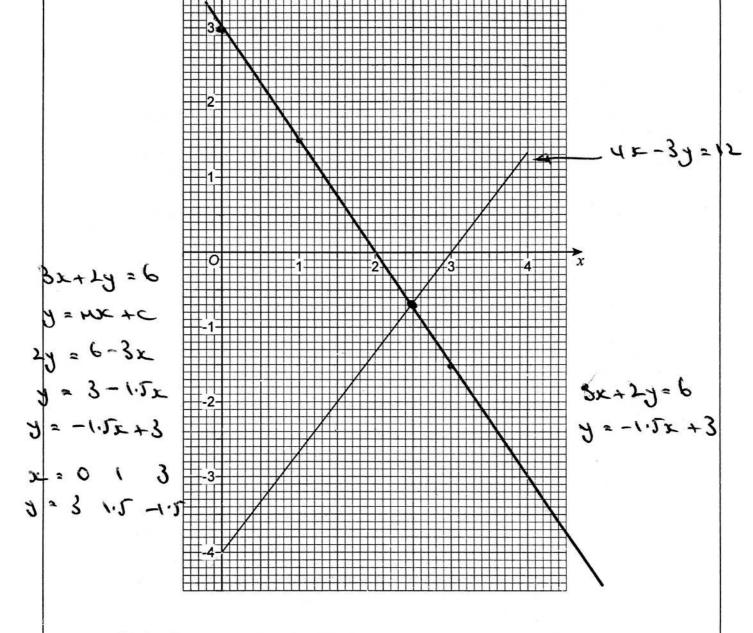
[1 mark]

Answer John

Reason greater no. of rolls (100)

Version 1.0





By drawing a second graph on the grid, work out an approximate solution to the simultaneous equations

$$4x - 3y = 12$$
 and  $3x + 2y = 6$ 

[3 marks]

Answer x = 2.5 y = -0.7

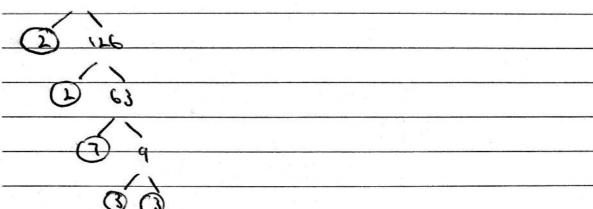
9 Written as the product of its prime factors

$$672 = 2^5 \times 3 \times 7$$

Write 252 as the product of its prime factors. 9 (a)

[2 marks]

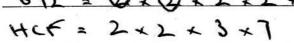




Answer  $252 = 2^{2} \times 3^{2} \times 7$ 

Work out the value of the highest common factor of 672 and 252 9 (b)

[1 mark]



Answer HCF = 84

Turn over for the next question

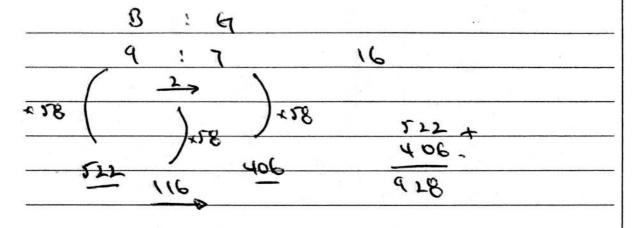
	10	At a	school
--	----	------	--------

number of boys: number of girls = 9:7

There are 116 more boys than girls.

Work out the total number of students at the school.

[3 marks]

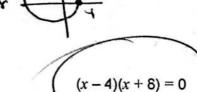


Answer 9 28

11 Circle the equation with roots 4 and -8

$$4x(x-8)=0$$

$$x^2 - 32 = 0$$



2=4

$$(x+4)(x-8)=0$$

[1 mark]

$$R = \frac{x^2}{y}$$

$$x = 3.6 \times 10^5$$

$$y = 7.5 \times 10^4$$

Work out the value of R.

Give your answer in standard form to an appropriate degree of accuracy.

[3 marks]

$$R = (3.6 \times 10^{5})^{2}$$
 1728000

= 1.728 x 106

= 1.7 × 106 (+0 18p)

Answer

balls.

13 Two spaceres have radii in the ratio 5:3

Circle the ratio of their volumes.

[1 mark]

5:3

15:9

25:9







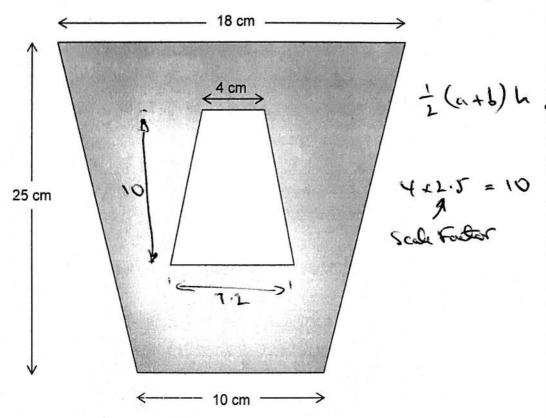
Vol 53: 33



Turn over for the next question



Not drawn accurately

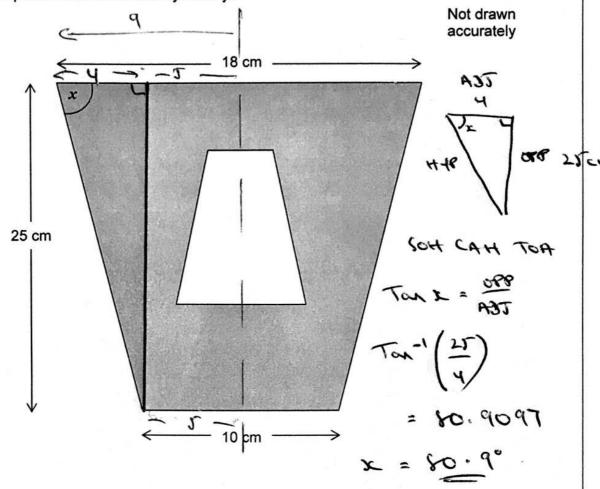


Show that the shaded area is 294 cm<sup>2</sup>

[4 marks]

Large - small = 310 - 16 = 294cm2

14 (b) The pattern has one line of symmetry.



Work out the size of angle x.	[3 marks]

Answer \_\_\_\_\_ degrees

15	Ann picks a 4-digit number.
10	Ann picks a 4-digit number.

The first digit is not zero.

The 4-digit number is a multiple of 5

How many different 4-digit numbers could she pick?

[3 marks]

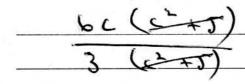
10,000 -		1627			
11000	∞∞9	+5	2	1100	
0					
4,000					

Answer	1800	
	, ,	

# 16 c is a positive integer.

Prove that	$6c^3 + 30c$	is an even number.
	$3c^2 + 15$	is all ever fluitiber

[3 marks]



2c	AQ	even	number	are a	m Diple	R
	de	ony r	reluce			V
 <i>c</i> • • • • • • • • • • • • • • • • • • •						

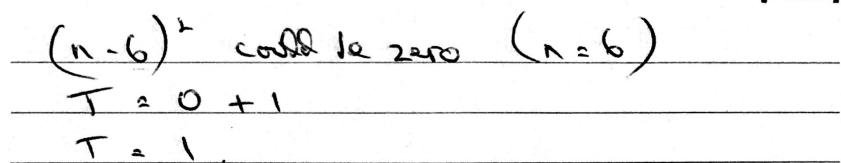
17	The distance from the Earth to the Sun is 93 million miles.	
	Assume	
	it takes 365 days for the Earth to travel once around the Sun	
	the Earth travels in a circle with the Sun at the centre.	
17 (a)	Work out the average speed of the Earth in miles per hour.	1 marks]
	Speel = The.	/
~	intance = 2TT	/
J	towals = 277 93000000	$\mathcal{I}$
	= 544336233.6 IANS	
	5 2 8 d 2 2 6 5 2 2 · P (JUD)	
	ANC.	-
	Speed = 365 x 24	
	= 66705 - 04949	
	Answer 66705 miles per hour	
17 (b)	It actually takes $365\frac{1}{4}$ days for the Earth to travel once around the Sun.	
	How does this affect your answer to part (a)?	[1 mark]
	Speed will be rlower 5.8x108	
	365-25 224 365 224	
	PE1EN. 13 PE510.02	

- In the formula  $T = (n-6)^2 + 1$  n is a positive integer.
- **18** (a) Kim says,

"The value of T is always greater than 1 because  $(n-6)^2$  is always greater than 0"

Comment on her statement.

[1 mark]



**18** (b) What is the only value of T that is a square number?

[1 mark]

when 
$$(n-6)^{+}=0$$
  
then  $T=1$  is a square number

Answer \_\_\_\_\_

19	f(x) =	3x

Circle the expression for  $f^{-1}(x)$ 

[1 mark]

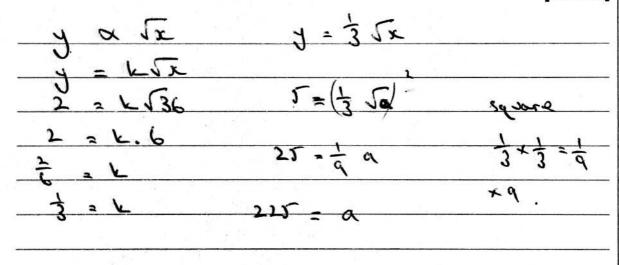


20 y is directly proportional to  $\sqrt{x}$ 

x	36	а
у	2	5

Work out the value of a.

[4 marks]



Answer \_\_\_\_

21	A company makes boxes of cereal.
	A have visually contains 450 grams of a

A box usually contains 450 grams of cereal.

Here are two options for a special offer.

# Option B

Usual amount of cereal 15% off the price

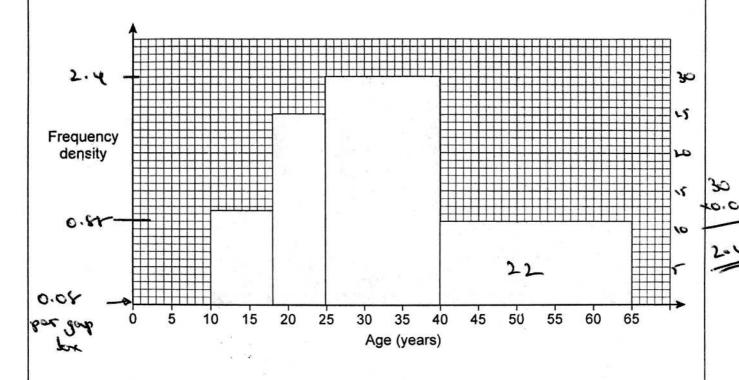
Which option is the better value for the customer?

You must show your working.

[3 marks]

aprion A	option B
540g for £1	4509
(100g)	450 for 85p.
price per gran	price per gram
100 = 0.181185	N 0.18888
540	450
Dor retter A nutgo	હિશ્

The histogram shows the ages, in years, of members of a chess club.



There are 22 members with ages in the range  $40 \le age \le 65$ 

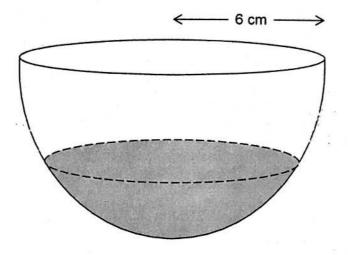
Work out the number of members with ages in the range 25 ≤ age < 40

 $FD = \frac{F_{neq}}{Clanwill}$   $= \frac{22}{27} = 0.8$   $= \frac{24}{27} = \frac{F_{neq}}{17}$   $= \frac{24}{27} = \frac{F_{neq}}{17}$ 

Answer 36 manders 25 5 age < 40

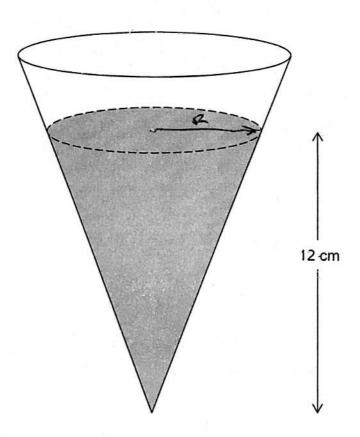
A bowl is a hemisphere with radius 6 cm

Water fills two-fifths of the volume of the bowl.



The water is poured into a hollow cone.

The depth of the water in the cone is 12 cm



Volume of a sphere =  $\frac{4}{3}\pi r^3$  where r is the radius.

Volume of a cone =  $\frac{1}{3}\pi r^2 h$  where r is the radius and h is the perpendicular height

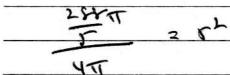
Work out the radius of the surface of the water in the cone.

[4 marks]

Total vol = 
$$\frac{1}{2} \left( \frac{4}{3} \pi \Gamma^3 \right)$$

Larringhere

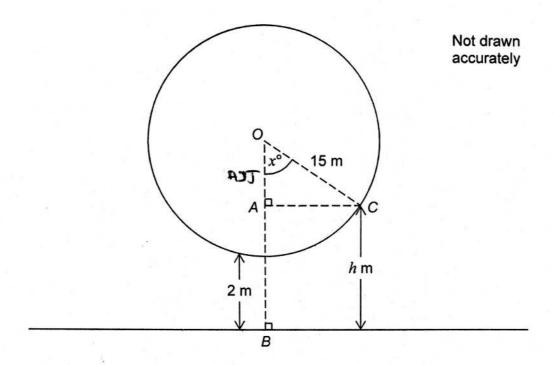
=  $\frac{1}{2} \left( \frac{4}{3} \pi \Gamma^3 \right)$  Vol Buster



A Big Wheel is modelled as a circle with centre O and radius 15 metres.

The wheel turns in an anticlockwise direction.

The lowest point on the wheel is always 2 metres above horizontal ground.



**24** (a) C is a point on the wheel, h metres above horizontal ground.

Angle  $COB = x^{\circ}$ 

Show that  $h = 17 - 15 \cos x^{\circ}$ 

COS x = 12

SOH CAH TOA

(Tradice + Labour grown

Height 17 - 15cogx

Vrw(x = ADT.

283

24 (b) D is a point on the wheel.

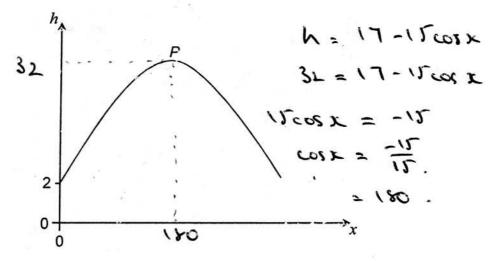
> Angle DOB = 120° Not drawn 4-18 accurately 17 SOH CAH TOA

Work out the height of D above horizontal ground.

 $5 \text{ in } 30^{\circ} = \frac{\text{ope}}{15}$  7.5 = ope 0 = 7.5 + 17[2 marks]

Answer 24.5 metres

Here is a sketch of the graph  $h = 17 - 15 \cos x^{\circ}$  for one countries turn of the wheel. 24 (c) P is the highest point on the graph.



Work out the coordinates of P.

[2 marks]

8300/2H

- 25  $2x^2 6x + 5$  can be written in the form  $a(x b)^2 + c$  where a, b and c are positive numbers.
- **25** (a) Work out the values of a, b and c.

[3 marks]

$$\frac{2x^{2}-6x+5}{2(x^{2}-3x)+5} \qquad (x-\frac{3}{2})(x-\frac{3}{2})$$

$$\frac{2(x^{2}-3x)^{2}+5}{2(x-\frac{3}{2})^{2}-\frac{9}{4}}+5$$

$$\frac{2(x-\frac{3}{2})^{2}-\frac{9}{4}+5}{2(x-\frac{3}{2})^{2}-\frac{9}{4}+\frac{10}{2}}$$

$$2(x-\frac{3}{2})^{2}+\frac{1}{2}$$

$$b = \frac{3}{2}$$

$$c = \frac{1}{2}$$

Using your answer to part (a), or otherwise, solve  $2x^2 - 6x + 5 = 8.5$ 25 (b)

$$2x^2 - 6x + 5 = 8.5$$

[3 marks]

$$2\left(x-\frac{3}{2}\right)^{2}=8$$

$$\int (x-\frac{3}{2})^2 = 4$$

$$2 + 2 + 2 + \frac{3}{2}$$
  $3 + 2 + \frac{3}{2}$ 

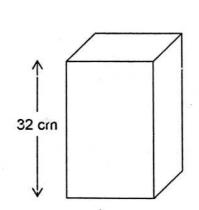
Answer \_\_\_\_\_

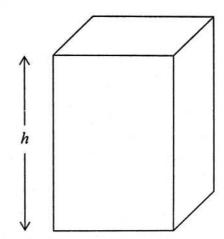
Turn over for the next question

26 Two boxes are made with card							
	26	TWO	havas	250	mada	mith	aard

The boxes are similar cuboids.

The smaller box has height 32 cm





It takes 44% more card to make the larger box.

Work out the height, h, of the larger box.

[4 marks]

Cargar	lox 2	1.44 smaller	= Areco	rade for
1.44	2 K	Leiald =	3) 4 1.2	
51.44	= k	-	38.4	-
(.7	= 1_			2.0

Answer 38.4 cm

**END OF QUESTIONS** 

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